## QACTEX Learning

EA-1 Exams \& Solutions

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An EA Exam

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## CONDTIONS GENERALLY APPLICABLE TO ALL EA-1 EXAMINATION QUESTIONS

If applicable, the following conditions should be considered a part of the data for each question, unless otherwise stated or implied.
(1) The normal retirement age is 65 .
(2) Retirement pensions commence at normal retirement age and are paid monthly for life at the beginning of each month.
(3) There are no pre-retirement death or disability benefits.
(4) Actuarial equivalence is based on the mortality table and interest rate assumed for funding purposes.
(5) Interest rates that are compounded more frequently than annually are expressed as nominal rates.
(6) Where multiple lives are involved, future lifetimes are assumed to be independent of each other.
(7) The term "gross single premium" is equivalent to "contract single premium;" the term "net single premium" is equivalent to "single benefit premium;" the term "gross annual premium" is equivalent to "annual contract premium;" the term "net annual premium" is equivalent to "annual benefit premium."
(8) There are no policy loans in effect.
(9) For a bond, the face amount and the redemption value are the same.
(10) Interest rate equals yield rate.
(11) The term "duration" means "Macaulay duration".

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## Data for Question 1 (3 points)

A table of $s_{n}$ at $5.0 \%$ is to be constructed on a computer using the following recursive formula:

$$
\begin{aligned}
& s_{11}=1 \\
& s_{\overline{n+1}}=1.05 s_{n}+1 \quad n \geq 1
\end{aligned}
$$

However, an error occurred and the following incorrect recursive formula was used:

$$
\begin{aligned}
& s_{\overline{1}}=1 \\
& s_{\overline{n+1}}=1.05 s_{\bar{n}}+0.1 \quad n \geq 1
\end{aligned}
$$

$\boldsymbol{X}=$ the value produced for $s_{20}$ using the incorrect recursive formula.

## Question 1

In what range is $\boldsymbol{X}$ ?
(A) Less than 5.60
(B) 5.60 but less than 5.70
(C) 5.70 but less than 5.80
(D) 5.80 but less than 5.90
(E) 5.90 or more

Data for Question 2 (3 points)
Selected annuity values:

$$
\begin{aligned}
\ddot{a}_{\overline{n+2}} & =14.030 \\
\ddot{s}_{\bar{n}} & =52.344
\end{aligned}
$$

$X=$ the effective annual interest rate.

## Question 2

In what range is $\boldsymbol{X}$ ?
(A) Less than $5.00 \%$
(B) $5.00 \%$ but less than $5.25 \%$
(C) $5.25 \%$ but less than $5.50 \%$
(D) $5.50 \%$ but less than $5.75 \%$
(E) $5.75 \%$ or more

## Data for Question 3 (3 points)

Terms of a perpetuity:
Frequency of payments Annual, payable at the end of each year
Payment amounts
$\$ 1$ at the end of years $1,4,7, \ldots$
$\$ 2$ at the end of years $2,5,8, \ldots$
$\$ 3$ at the end of years $3,6,9, \ldots$
Interest rate: $5.0 \%$ per year, compounded semiannually
$X=$ the present value of the perpetuity.

## Question 3

In what range is $\boldsymbol{X}$ ?
(A) Less than $\$ 25$
(B) $\$ 25$ but less than $\$ 30$
(C) $\$ 30$ but less than $\$ 35$
(D) $\$ 35$ but less than $\$ 40$
(E) $\$ 40$ or more

Data for Question 4 (3 points)
Provisions of an annuity-immediate:

| Periodic payment | $\$ 150$ |
| :--- | :--- |
| Payment frequency | Quarterly |
| Term | 5 years |

Interest rate: $8.00 \%$ per year, compounded semi-annually
$X=$ the present value of this annuity.

Question 4
In what range is $X$ ?
(A) Less than $\$ 2,405$
(B) $\$ 2,405$ but less than $\$ 2,455$
(C) $\$ 2,455$ but less than $\$ 2,505$
(D) $\$ 2,505$ but less than $\$ 2,555$
(E) $\$ 2,555$ or more

## Data for Question 5 (4 points)

Terms of a loan:
Term $\quad 36$ months
Repayments Level monthly, payable at the end of each month Interest rate $18.0 \%$ per year, compounded monthly
$X=$ the ratio of cumulative interest repaid to cumulative principal repaid immediately following the 24th payment.

## Question 5

In what range is $\boldsymbol{X}$ ?
(A) Less than 0.40
(B) 0.40 but less than 0.42
(C) 0.42 but less than 0.44
(D) 0.44 but less than 0.46
(E) 0.46 or more

## Data for Question 6 (3 points)

Terms of a loan:

| Amount borrowed | $\$ 10,000$ |
| :--- | :--- |
| Repayments | Level annual, payable at the end of each year |
| Interest rate | $4.0 \%$ per year, compounded annually |

The interest portion of the fourth payment is $\$ 225$.
$X=$ the principal portion of the fourth payment.

Question 6
In what range is $\boldsymbol{X}$ ?
(A) Less than $\$ 1,225$
(B) $\$ 1,225$ but less than $\$ 1,325$
(C) $\$ 1,325$ but less than $\$ 1,425$
(D) $\$ 1,425$ but less than $\$ 1,525$
(E) $\$ 1,525$ or more

## Data for Question 7 (3 points)

Terms of a 10-year bond:

| Face amount | $\$ 1,000$ |
| :--- | :--- |
| Redemption amount | $\$ 1,000$ |
| Coupon rate | $4.0 \%$ per year, payable semi-annually |
| Yield rate | $5.0 \%$ per year, compounded semi-annually |

$\boldsymbol{X}=$ the total investment return to the purchaser over the lifetime of the bond.

## Question 7

In what range is $\boldsymbol{X}$ ?
(A) Less than $\$ 350$
(B) $\$ 350$ but less than $\$ 400$
(C) $\$ 400$ but less than $\$ 450$
(D) $\$ 450$ but less than $\$ 500$
(E) $\$ 500$ or more

